

On the p -Rank of the Incidence Matrix of a Balanced or Partially Balanced Incomplete Block Design and its Applications to Error Correcting Codes

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