

AN EXTREMAL PROBLEM ON THE CLASSICAL CARTAN DOMAINS, III

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1. Let D_1, \dots, D_N be the classical Cartan domains. We define the numbers n_{D_v} and λ_{D_v} as follows:

$$n_{D_v} = \begin{cases} rs & , \text{ if } D_v = R_I(r, s), \\ \frac{p(p+1)}{2} & , \text{ if } D_v = \hat{R}_{II}(p), \\ \frac{q(q-1)}{2} & , \text{ if } D_v = R_{III}(q), \\ m & , \text{ if } D_v = R_{IV}(m), \end{cases}$$

and

$$\lambda_{D_v} = \begin{cases} \sqrt{s} & , \text{ if } D_v = R_I(r, s), \\ \sqrt{\frac{p+1}{2}} & , \text{ if } D_v = \hat{R}_{II}(p), \\ \sqrt{q-1} & , \text{ if } D_v = R_{III}(q) \text{ and } q \text{ is even,} \\ \sqrt{q} & , \text{ if } D_v = R_{III}(q) \text{ and } q \text{ is odd,} \\ \sqrt{m} & , \text{ if } D_v = R_{IV}(m), \end{cases}$$

where

$$R_I(r, s) = \{Z = (z_{ij}) : I - Z\bar{Z}' > 0, \text{ where } Z \text{ is an } r \times s \text{ matrix}\}, \quad (r \leq s),$$

$$R_{II}(p) = \{Z = (z_{ij}) : I - Z\bar{Z}' > 0, \text{ where } Z \text{ is a symmetric matrix of order } p\},$$

$$\hat{R}_{II}(p) = \{Z = (z_{ij}) : z_{ij} = \sqrt{2} x_{ij} \ (i \neq j), \ z_{ii} = x_{ii}, \text{ where } X = (x_{ij}) \in R_{II}(p)\},$$

$$R_{III}(q) = \{Z = (z_{ij}) : I - Z\bar{Z}' > 0, \text{ where } Z \text{ is a skew-symmetric matrix of order } q\},$$

$$R_{IV}(m) = \{z = (z_1, \dots, z_m) : 1 + |zz'|^2 - 2z\bar{z}' > 0, \ 1 - |zz'| > 0\}.$$

We set

$$D = \lambda_{D_1} D_1 \times \dots \times \lambda_{D_N} D_N, \quad n = n_{D_1} + \dots + n_{D_N},$$

and denote the family of holomorphic mappings from D into the unit hyperball