

Erratum to “Expansive invertible oneshided cellular automata”

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In our paper [BM], a part of the proof of Proposition 3.2 is incorrect. (The statement of Proposition 3.2 is correct.) The error in the proof is the claim that the follower set cover of a nonSFT sofic shift cannot be irreducible. A counterexample to the claim is the sofic shift presented by the labeled graph with adjacency matrix $\begin{pmatrix} a+b & c+d \\ b & a \end{pmatrix}$. For this shift, the predecessor set cover is also irreducible. We thank Ulf Fiebig for pointing out our error and for providing the counterexample, which is part of a forthcoming work on the possible structures of Krieger covers [F].

The part of Proposition 3.2 which requires a correct proof is the claim that a sofic shift whose bilateral dimension group has rank one must be a shift of finite type. The application of this claim in [BM] is a special case of the subsequent decisive result of M. Nasu [N] that all expansive invertible oneshided onedimensional cellular automata are shifts of finite type. Nevertheless, because Proposition 3.2 is of independent interest and because we want to maintain the unified framework of the proofs in [BM], we will give a correct proof of the claim here.

A word W is a *synchronizing word*, or *Markov magic word*, for a subshift if whenever there are points x and y in the subshift and a nonnegative integer n such that $x[0, n] = y[0, n] = W$, then the bisequence $x(-\infty, -1]Wy[n+1, +\infty)$ is a point in the subshift. Every sofic shift contains synchronizing words [K, Observation 6.1.5]. Therefore the proof of Proposition 3.2 is repaired by the following proposition (which applies more generally to the large and interesting class of subshifts with a synchronizing word [BH], [FF]).

PROPOSITION. *Suppose S is a subshift with a synchronizing word and the group $\text{Bilat}(S)$ has rank one. Then S is a shift of finite type.*

PROOF. We first present the group $\text{Bilat}(S) = \mathbf{ZCO}(X)/K(S)$ of [BM] as a certain direct limit group $G = \lim G_n$. Define an equivalence relation on S -words as follows: $[W] = [W']$ if the words W and W' have equal length and for all words A and B , AWB is an S -word if and only if $AW'B$ is an S -word. Given a positive integer n , let G_n be the free abelian group whose generating set is the set E_n of equivalence classes of S -words of length $2n+1$. Define the system of group homomorphisms $\pi_{n, n+k} : G_n \rightarrow G_{n+k}$ determined by $[x_{-n} \cdots x_n] \mapsto \sum [ax_{-n} \cdots x_n b]$, where the sum is over the pairs (a, b) such that a and b have length k and $ax_{-n} \cdots x_n b$ is an S -word. The group G is the direct limit group obtained from this system of homomorphisms, and $\text{Bilat}(S)$ is