

Concerning Two Properties of Connectivity Functions

Let X and Y be topological spaces and let $f:X \rightarrow Y$. Then:

- D. : f is a Darboux function if $f(C)$ is connected whenever C is connected in X .
- Conn. : f is a connectivity function if the graph of f restricted to C , denoted by $f|_C$, is connected in $X \times Y$ whenever C is connected in X .
- A.C. : f is an almost continuous function if $U \subset X \times Y$ is any open set containing the graph of f , then U contains the graph of a continuous function $g:X \rightarrow Y$.
- Ext. : f is an extendable function if there exists a connectivity function $g:X \times [0,1] \rightarrow Y$ such that $f(x) = g(x,0)$ for each x in X .

Let $f:[a,b] \rightarrow R$ be a function. Then:

- P.R. : f has a perfect road if for each x in $[a,b]$ there exists a perfect set P having x as a bilateral limit point such that $f|_P$ is continuous at x . If x is an endpoint, then the bilateral condition is replaced with a unilateral condition.

For real-valued functions defined on an interval $[a,b]$ we have only the following implications among the classes of functions defined above.