

Jónsson algebra is explained in detail. There is also an application to the calculation of the cofinality of partial orders of the form  $([\lambda]^\kappa, \subseteq)$ , where  $[\lambda]^\kappa$  is the set of all subsets of  $\lambda$  that have cardinality  $\kappa$ . Specifically, it is shown that for any infinite cardinal  $\kappa$  and any non-zero  $\alpha < \kappa$ ,  $\text{cf}([\kappa^{+\alpha}]^\kappa, \subseteq) = \max \text{pcf}\{\kappa^{+(\beta+1)} : \beta < \alpha\}$ . This is one example from a rich collection of theorems in *Cardinal arithmetic* and subsequent works of Shelah concerning the relationship between covering numbers and pcf's. These results are quite useful in cardinal arithmetic and related areas. In addition to Shelah's original works, a good source for further theorems relating cofinalities and pcf's is an elegant recent article on pcf theory by Uri Abraham and Menachem Magidor, *Cardinal arithmetic*, which is available at [www.cs.bgu.ac.il/~abraham/math.html](http://www.cs.bgu.ac.il/~abraham/math.html) and which will appear in the *Handbook of set theory*, to be published by Kluwer.

Chapter 9 covers Shelah's pp function. For singular cardinals  $\lambda$ ,  $\text{pp}(\lambda)$  is the supremum of all cardinals of the form  $\text{cf}(\prod a/D)$ , where  $a$  is a cofinal set of regular cardinals in  $\lambda$ ,  $a$  has cardinality  $\text{cf}(\lambda)$ , and  $D$  is an ultrafilter on  $a$  that contains all final segments of  $a$ . In *Cardinal arithmetic*, Shelah proposes that  $\text{pp}(\lambda)$  is the "true"  $\lambda^{\text{cf}\lambda}$ . One advantage it has over  $\lambda^{\text{cf}\lambda}$  is that its value is much harder to change by forcing. For example, the results of Chapter 7 imply that  $\text{pp}(\aleph_\omega) < \aleph_{\omega_4}$ . Versions of the Galvin–Hajnal theorems from Chapter 2 are established for the pp function.

A couple of the proofs in the text contain minor gaps. (1) On page 109, the proof of Lemma 2.2.1 (the case of the free set lemma where the domain is a set  $A$  of regular cardinality  $\kappa$  and the set mapping  $K$  satisfies  $|K(a)| < \lambda < \kappa$  for all  $a \in A$ ) seems to go wrong at the end. The  $\subseteq$ -maximal set  $\mathcal{P}$  of pairwise disjoint popular sets at the end of the proof could be simply  $\{A\}$  (if each  $K(a)$  is non-empty). This is easily repaired, but the entire argument can be worded more succinctly: denoting  $X \cup \bigcup \{K(x) : x \in X\}$  by  $H[X]$ , for  $\xi < \lambda$ , inductively choose a maximal independent subset  $X_\xi$  of  $A \setminus \bigcup_{\eta < \xi} H[X_\eta]$ . Then  $|X_\xi| = \kappa$  for some  $\xi < \lambda$ , for otherwise  $\bigcup_{\xi < \lambda} H[X_\xi]$  has size  $< \kappa$  and for any  $a \in A$  not in this set the maximality of each  $X_\xi$  and the fact that  $a \notin K(x)$  for any  $x \in X_\xi$  gives  $K(a) \cap X_\xi \neq \emptyset$  for all  $\xi < \lambda$ , contradicting  $|K(a)| < \lambda$ . (2) The proof of Theorem 9.2.4, on page 277, introduces a club-guessing sequence for  $S = \Sigma_{\mu, \aleph_0}$ , using Lemma 4.5.3 to justify its existence. But Lemma 4.5.3 assumes that  $S$  is contained in a set of the form  $\Sigma_{\kappa, \mu}$  where  $\mu$  is uncountable. The proof of Lemma 4.5.3 for  $\mu = \aleph_0$  is similar but somewhat harder. In *Cardinal arithmetic* the required result is Claim 2.3(2) of Chapter III. It can also be found in a useful preprint of Menachem Kojman entitled *The A, B, C of pcf: a companion to pcf theory, part I*, available at the time of writing of this review at [www.cs.bgu.ac.il/~kojman](http://www.cs.bgu.ac.il/~kojman). This preprint also contains several other club-guessing principles and develops the basic results of pcf theory using the coherent sequences that are discussed in *Cardinal arithmetic* in §0 of the *Analytical guide* on page 436.

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STEVO TODORCEVIC. *Topics in topology*. Lecture notes in mathematics, vol. 1652. Springer, Berlin, Heidelberg, New York, etc., 1997, viii + 153 pp.

Faithfully to its title, this book is an author's personal selection of several diverse topics in topology. It grew out of a set of lecture notes from a graduate course given by Todorćević at the University of Toronto during the fall of 1995. The book consists of four independent chapters, each covering a different "topic" in general topology.

The first chapter is the longest and most extensive one. It is entitled *Compact sets in function spaces* and it considers  $C_p(X)$ , the space of continuous functions with respect to the topology of pointwise convergence on a Polish space  $X$ . The goal of Chapter I is to give