

CORRIGENDUM TO: “RELATION ALGEBRA REDUCTS OF
 CYLINDRIC ALGEBRAS AND COMPLETE REPRESENTATIONS”

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Thanks to Tarek Sayed Ahmed for bringing an important error in [1] to my attention. In the abstract of [1], the fourth displayed equation claims wrongly that “ \exists has a winning strategy in $H(\text{At}(A))$ implies $A \in \mathfrak{Ra}(\mathbf{CA}_\omega)$ ”. Unfortunately, this turns out to be false. This line should be replaced by the weaker claim: “ \exists has a winning strategy in $H(\text{At}(A))$ implies there is $C \in \mathbf{RCA}_\omega$ such that $\text{At}(\mathfrak{Ra}C) \cong \text{At}(A)$.” This weaker claim is already proved in [1, theorem 39].

Two lines down, in the final displayed equation of the abstract, the line “ $\mathfrak{RaRCA}_\gamma \subseteq K \subseteq S_c\mathfrak{RaCA}_5$ ” should be replaced by “ $S_c\mathfrak{RaRCA}_\gamma \subseteq K \subseteq S_c\mathfrak{RaCA}_5$.” Whether \mathfrak{RaRCA}_ω is elementary or not is open.

These changes in the abstract require slight changes to theorem 39 and definition 40 and a more substantial change to theorem 45. Theorem 39 should be slightly strengthened as follows. “Let $\gamma \geq 5$, let α be a countable relation algebra atom structure. If \exists has a winning strategy in $H(\alpha)$ then there is $C \in \mathbf{RCA}_\gamma$ such that $\mathfrak{Ra}(C)$ is atomic and $\text{At}\mathfrak{Ra}(C) \cong \alpha$. The proof already shows that $C \in \mathbf{RCA}_\omega$ and we may extend the result to ordinals $\gamma > \omega$ by redefining U_α to be $\{f \in {}^\gamma\text{nodes}(N_a) : \{i < \gamma : f(i) \neq g(i)\} \text{ is finite}\}$.”

In [1, definition 40], the final line “Let A be the complex algebra over α (so the domain consists of arbitrary sets of atoms).” should be replaced by “Let A be the *term algebra* of α —the countable subalgebra of the complex algebra of α , generated by α .”

Theorem 45 is wrong. The correct statement should be “Let $\gamma \geq \omega$ and let K be any class of relation algebras such that $S_c\mathfrak{RaCA}_\gamma \subseteq K \subseteq S_c\mathfrak{RaCA}_5$. Then K is not closed under elementary subalgebras hence K is not an elementary class.” The proof of this revised theorem can be simplified and completed without the use of the hypernetwork game H . Here, however, we aim to minimise the size of this errata. Accordingly, the corrected proof to theorem 45 is:

“Let A be the rainbow algebra of definition 40 and let $A' \succeq A$ be the countable elementary extension given by lemma 44. Since \exists has a winning strategy in $H(A')$, by theorem 39 there is $C \in \mathbf{RCA}_\gamma$ such that $\text{At}\mathfrak{Ra}(C) \cong \text{At}(A')$. Let $C' \supseteq C$ be the McNeille completion of C , this is a complete cylindric algebra and $\text{At}\mathfrak{Ra}(C') = \text{At}\mathfrak{Ra}(C)$. Then $A' \subseteq_c \mathfrak{Cm}(\text{At}(A')) = \mathfrak{Ra}(C')$, by lemma 15, so $A' \in S_c\mathbf{RCA}_\gamma$. But $A \notin K$, by lemma 41.”

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