Errata

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This is to correct [2]. As declared at the start of Section 5 in [2], Lemma 5.8 there was taken from Kempf's article [3, Prop. 6]. However, the way of citing was erroneous. In Kempf's original paper, the intersection of two quasi-compact open subsets is assumed to be again quasi-compact. But in our Lemma 5.8 this assumption has been erroneously omitted and, as the following example shows, the lemma in its present form is wrong. The correct statement of Lemma 5.8 follows.

LEMMA 5.8. *Let X be a topological space. Assume that X has an open basis consisting of quasi-compact open subsets and that the intersection of two quasi-compact open subsets is quasi-compact. Let U be a quasi-compact open subset of X and let $(\mathcal{M}_\lambda)$ be a pseudo-filtered inductive system of sheaves of abelian groups on X. Then the canonical map*

$$\varinjlim \Gamma(U, \mathcal{M}_\lambda) \to \Gamma(U, \varinjlim \mathcal{M}_\lambda)$$

is an isomorphism.

In the statement of Corollary 5.10 we need to assume that X is quasi-separated; in its proof, U should be assumed to be affine.

In Lemma 5.11 we use Corollary 5.10, but since an immersion is quasi-separated, the lemma requires no modification.

EXAMPLE 1. Let $P = \mathbb{N} \cup \{a, b\}$ be a partially ordered set defined by the following conditions:

- any two elements of $\mathbb{N}$ are incomparable;
- a and b are incomparable;
- any element of $\{a, b\}$ is smaller than each element of $\mathbb{N}$.

Letting a filter (or an increasing subset) be an open subset, P is a topological space. For $x \in P$, let $V_x := \{y \in P \mid y \geq x\}$ be the principal filter generated by x. Note that V_x is quasi-compact and that $\{V_x \mid x \in P\}$ is an open basis of P. Note further that $P = V_a \cup V_b$ is also quasi-compact. However, the intersection $V_a \cap V_b$ of the two quasi-compact open subsets V_a and V_b is $\mathbb{N}$, which is not quasi-compact.

Let k be a field. For $n \in \mathbb{N}$, define a sheaf M_n on P as follows:

- $\Gamma(V_m, M_n) = k$ if $m \geq n$, and $\Gamma(V_m, M_n) = 0$ if $m < n$;
- $\Gamma(V_a, M_n) = \Gamma(V_b, M_n) = k$;