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THE PRAGMATICS OF MONADIC QUANTIFICATION

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I. Pragmatics of Truth Functions

1. Sentential Interpretations In [2] the truth functional logic of a set S of sentences was characterized pragmatically with respect to a set U of users of S, a set T of times of valuation of sentences of S, a set C of conditions of such valuations, and a set V of pragmatic values. Pragmatic interpreting functions were defined with domain $U \times T \times C \times S$ and range V, so that these functions induced a Boolean structure on S. In the present paper, pragmatic interpreting functions are defined whose applicability is more general and whose structure is more fundamental from a pragmatic point of view than those of [2].

Let L be the set of all expressions of some language. More precisely, let L be the set of all concatenates of a set of expressions which may be regarded as the alphabet of some language. Abstractly, L is any set of objects generated from a given finite set L, by a binary operation satisfying the properties of concatenation.

Let C be a set of conditions of valuation of the expressions of L. No assumptions about the nature or structure of the elements of C are required in the definition of pragmatic interpreting functions; abstractly, C is any set. Intuitively, C may be regarded as a set of conditions which may be conjointly realized as an experimental state, or partial state, of the world, identifiable by the users of L. On the basis of sets of such conditions, the expressions of L assume pragmatic values for the users of L. In being so valued, the expressions of L are "confronted with the world". The set C may be regarded as the total evidence available to the users of L. Let \mathbb{C} be the set of all subsets of C.

Let $V = \{0, 1, 2\}$ be the set of pragmatic values which may be assumed by the expressions of L. No further structure on V need be assumed in the definition of pragmatic interpreting functions; abstractly, V is any threemembered set. Intuitively, the element 0 may be regarded as the value assigned to an expression of L under a given set of conditions, when the expression is *rejected* under that set of conditions. The value 1 is assigned