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Predication in the Logic of Terms

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Abstract The paper contrasts modern predicate logic (MPL) and term/ functor logic (TFL) on predication. A predication in TFL consists of two terms and a "logical copula" that has formal properties such as symmetry or transitivity. The I-functor in 'PiS' (the old form of '(some) S is P') is symmetrical, behaving like the plus sign of high school algebra; TFL transcribes 'PiS' as 'P + S'. The transitive A-functor in 'PaS' (every S is P) is minuslike: 'P - S = -((-P) + S)' represents the equivalence of 'PaS' to 'not ((-P)iS)'. In propositional logic 'q + p' transcribes 'p & q' and 'q - p' transcribes 'q if p'; thus 'q - p = -((-q) + p)' is the algebraic form of 'p → q = -(p & (-q))'. TFL applies to relational statements of any complexity. E.g., to show the inconsistency of 'every A is B and something R to an A is not R to a B' we add '-(R + B) + (R + A)' to 'B - A' to get the contradiction '-(R + B) + (R + B)'. The predicative functors are shown to give TFL a slight advantage over MPL in expressive and inference power when dealing with singular statements.

The copula has no place in the language of modern logic. It will be shown that a significant price in the hard currency of inference power is being paid because of its absence. A properly formulated term logic, extended to handle relational inference, is both syntactically simpler and inferentially more powerful. But, historically, term logic took a wrong turn and we begin with that.

I Traditional syllogistic logic with its A, E, I, and O classification of categorical statements has a distinctive syntax that was not properly understood by its practitioners. Confusion arose because most syllogists favored a parsing of

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