

THE RULE OF EXCISION IN POSITIVE IMPLICATION

IVO THOMAS

The point made in [1] that the rule of excision

**RE:**  $\vdash \alpha, \vdash \phi (C \alpha \beta) \rightarrow \vdash \phi (\beta)$

can be more powerful than the rule of detachment

**RD:**  $\vdash \alpha, \vdash C \alpha \beta \rightarrow \vdash \beta$

is to be made with great economy in the context of positive implication. Assuming **RE**, substitution and the axiom

1.  $CCpCqrCCpqCpCsr$

we have

\*2.  $CCpCqrCCpqCpr$  [1 *s*/1, **RE**]

3.  $CCqrCqCsr$  [1 *p*/1, **RE**]

\*4.  $CrCsr$  [3 *q*/1, **RE**]

and **RD** as a special case of **RE**, thus having the positive system. But the matrix **MI**

<b>MI</b>	C	0	1	2
	*0	0	1	1
	1	0	0	1
	2	0	0	0

<b>MII</b>	C	0	1	2
	*0	0	2	2
	1	0	2	0
	2	0	0	0

which is hereditary under **RD**, verifies 1 and rejects 2;

$$CC1C12CC11C12 = CC11C01 = C0C01 = 1.$$

If interest of the system is disregarded, the point can be proved with maximum economy by excising *s* from 4 to obtain 5. *Crr*; but the matrix **MII** shows that 5 is independent of 4 and **RD**.

REFERENCE

[1] Angell, R. B., The sentential calculus using rule of interference  $R_e$ , *The Journal of Symbolic Logic*, vol. 25 (1960), p. 143.

*Blackfriars*  
*Oxford, England*

Received January 31, 1962