

## A Note Concerning the Notion of Mereological Class. Postscript

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Since the publication of my note concerning the notion of mereological class [1] I have noticed that a system of mereology—I shall refer to it as System  $\mathfrak{B}_1$ —can be based on the following single axiom:

$$\mathbf{B}_1\mathbf{A1} \quad [AB] \ddot{::} A \varepsilon el(B) .\equiv :: [\exists a] \ddot{::} B \varepsilon a :: [CD] \ddot{::} [E] \ddot{::} E \varepsilon C .\equiv :: [F] \ddot{::} [\exists G] . G \varepsilon el(E) . G \varepsilon el(F) .\equiv :: [\exists HI] . H \varepsilon a . I \varepsilon el(F) . I \varepsilon el(H) \ddot{::} B \varepsilon el(C) . B \varepsilon el(D) \ddot{::} \supset . A \varepsilon el(D).$$

In  $\mathbf{B}_1\mathbf{A1}$ , just as in  $\mathbf{BA1}$ , which is the axiom of System  $\mathfrak{B}$ ,  $\mathbf{E2}$  is embedded as the definition of the notion of mereological class, but  $\mathbf{B}_1\mathbf{A1}$  is shorter than  $\mathbf{BA1}$  by one ontological unit, and for this reason is of interest. It happens to be the shortest known single axiom for the notion of mereological elementhood.

The idea behind  $\mathbf{B}_1\mathbf{A1}$  becomes apparent as soon as one realises that the set of presuppositions  $\{\mathbf{B}_1\mathbf{A1}, \mathbf{E2}\}$  is inferentially equivalent to the set of presuppositions consisting of  $\mathbf{E2}$  and

$$\mathbf{B}_1\mathbf{A1.1} \quad [AB] \ddot{::} A \varepsilon el(B) .\equiv :: [\exists a] \ddot{::} B \varepsilon a : [C] \ddot{::} B \varepsilon el(KI(a)) . B \varepsilon el(C) .\supset . A \varepsilon el(C),$$

which is shorter than  $\mathbf{BA1.1}$ .

In order to prove that System  $\mathfrak{B}_1$  and System  $\mathfrak{B}$  are inferentially equivalent we first continue the deductions within the framework of System  $\mathfrak{B}$  as follows:

$$\begin{array}{ll} \mathbf{BT18} & [Aa] \ddot{::} A \varepsilon a .\supset . A \varepsilon el(KI(a)) \\ \textit{Proof:} & [Aa] \ddot{::} \text{Hp}(1) .\supset . \\ (2) & KI(a) \varepsilon KI(a) . \qquad \qquad \qquad [\mathbf{BT5}; 1] \\ & A \varepsilon el(KI(a)) \qquad \qquad \qquad [\mathbf{BT8}; 2; 1] \end{array}$$