

ANOTHER OBSERVATION ON THE DISTRIBUTION OF VALUES OF CONTINUED FRACTIONS $K(a_n/1)$

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Dedicated to the memory of Wolfgang J. Thron

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ABSTRACT. Jacobsen, Thron and Waadeland [1] determined results about the probability distribution for the values f of convergent continued fractions $K(a_n/1)$ in the case that the elements a_n are uniformly distributed both over the “real Worpitzky interval” $[-\rho(1-\rho), \rho(1-\rho)]$ and over the complex Worpitzky disk $\{z : |z| \leq \rho(1-\rho)\}$, for $0 < \rho \leq \frac{1}{2}$. This note explores extensions of some of those results in the case that the elements a_n are piecewise linearly distributed, with symmetry about zero, on the real Worpitzky interval.

1. Introduction. We are considering the values of continued fractions of the form

$$(1.1) \quad K_{n=1}^{\infty} \left(\frac{a_n}{1} \right) = \frac{a_1}{1+} \frac{a_2}{1+} + \cdots + \frac{a_n}{1+} \cdots$$

where the $a_n \neq 0$ are taken from the real Worpitsky interval

$$(1.2) \quad W = [-\rho(1-\rho), \rho(1-\rho)]$$

for $0 < \rho \leq \frac{1}{4}$. This interval is known to be a convergence region for (1.1). The values, f , of (1.1) are known to fill in the best limit value interval

$$(1.3) \quad V = [-\rho, \rho].$$

Here, however, we assume that the a_n have a known distribution on (1.2); the problem is to determine the distribution of the values,

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