

**A NOTE ON VALUATIONS, p -PRIMES
AND THE HOLOMORPHY SUBRING
OF A COMMUTATIVE RING**

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Introduction. In this note we use a recent result from the theory of valuations to identify p -primes in a special class of commutative rings. Our identification process will also provide the associated field with p -prime in each case. We refer the reader to [5], for all definitions pertaining to the p -prime invariants which, due to their length, will not be included here. At the conclusion of this paper we will apply our new information on the structure of all 0-primes to obtain a result on holomorphy subrings which is closely related to some earlier work by the author (see [4]).

We take this opportunity to introduce some notation which we will employ throughout this paper. Firstly, all rings will be understood to be commutative and unitary. For an arbitrary subset, S , of a ring R , set

$$I(R, S) = \{r \in R \mid rS \subseteq S\}$$

and

$$(R : S) = \{r \in R \mid rR \subseteq S\}.$$

We let $U(R)$ denote the group of units of R , and, in the case R is a domain, $\text{qf}(R)$ will represent the field of fractions of R . For I a prime ideal of R , let R_I be the localization of R at I . If R is assumed to be a local ring with maximal ideal M , then $k(R)$ and π will be used, respectively, to signify the residue class field R/M and the natural projection from R onto this field. Lastly, for $B \subseteq A$ we write $A \setminus B$ for $\{a \in A \mid a \notin B\}$.

1. Let R be a commutative ring. By a *valuation* of R we will mean a map $v : R \rightarrow G^*$, where G^* is a totally ordered abelian (possibly trivial) group which has been extended by ∞ , satisfying

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