

## $T$ -INVARIANT ALGEBRAS ON RIEMANN SURFACES II

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**1. Introductions.** In [7], T.W. Gamelin has introduced a subclass of planar uniform algebras which are by definition invariant under the so-called Vitushkin localization operators  $T_\varphi$ . In [7, 8] (see also [5]) he has developed the theory and, in particular, he has proved that a planar  $T$ -invariant algebra always has the Banach approximation property.

**DEFINITION.** A Banach space  $B$  has the *Banach approximation property* (BAP) if there exists a sequence  $\{P_n\}_{n=1}^\infty$  of finite dimensional linear operators on  $B$  such that  $P_n f$  converges to  $f$  for all  $f \in B$ .

More recently, J.A. Cima and R.M. Timoney [4] have shown that all planar  $T$ -invariant algebras also have the Dunford-Pettis property.

**DEFINITION.** A Banach space  $B$  has the *Dunford-Pettis property* (DPP) if, whenever  $\{f_n\}_{n=1}^\infty$  is a sequence in  $B^*$  tending weakly to 0, then

$$\lim_{n \rightarrow \infty} F_n(f_n) = 0.$$

We have, in [2], suggested a generalization of the Vitushkin operators to arbitrary non-compact Riemann surfaces and we have then proceeded to outline the development of a theory of  $T$ -invariant algebras in this context. We now continue our study by establishing the BAP and the DPP for  $T$ -invariant algebras on Riemann surfaces.

**REMARK.** In 1972, A. Sakai had already used the Behnke-Stein kernel (see [10]) in order to define a Cauchy transform and study some of the properties of the  $T_\varphi$ -operators on non-compact Riemann surfaces. We would like to thank the referee who has brought this to our attention.

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