

HYPERSURFACES OF LOW DEGREE

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1. Introduction

1.1. Statement of results. Let K be an algebraically closed field of characteristic 0. This paper is concerned with several aspects of the geometry of smooth hypersurfaces $X \subset \mathbb{P}_K^n$ over K whose dimensions are much larger than their degree (or, more generally, any hypersurface such that the codimension of the

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