

CHARACTERISTIC COHOMOLOGY OF DIFFERENTIAL SYSTEMS II: CONSERVATION LAWS FOR A CLASS OF PARABOLIC EQUATIONS

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