CORRECTION

PETER J. NICHOLLS

TO: Transitive horocycles for Fuchsian groups, Duke Math. J. 42 (1975), 307-312.

Let G be a Fuchsian group in the unit disc Δ with Ford fundamental region D and set $E = \{\xi \in \partial \Delta : \text{there exists } V \in G \text{ with } V(\xi) \in \overline{D}\}$. For $\xi \in \partial \Delta$ and r, 0 < r < 1, we denote by $C(\xi, r)$ that horocycle with Euclidean radius r and point at infinity ξ . The following is Theorem 1 of [1].

THEOREM. Let G be a Fuchsian group and $\xi \in \partial \Delta$ then the following statements are equivalent.

(i) $\xi \notin E$

(ii) For any r > 0 $C(\xi, r)$ contains an image of the origin in its interior.

(iii) There are images of $C(\xi, \frac{1}{2})$ with radii arbitrarily close to 1.

(iv) There exists a sequence of distinct transforms $\{V_n\}$ of G such that

 $|\xi - c(V_n)| = o(r(V_n)) \text{ as } n \to \infty$

where $c(V_n)$ and $r(V_n)$ denote respectively the center and radius of the isometric circle of V_n .

D. Sullivan has pointed out [3] that the proof of this theorem is invalid. The mistake occurs on p. 310 of [1]. It is asserted there that if, for some r > 0, $C(\xi, r)$ contains no equivalent of the origin in its interior, then there exists $R \ge r$ so that $C(\xi, R)$ contains an equivalent of the origin but its interior does not. There is another possibility which was overlooked by the author. It could happen that for some R > 0, $C(\xi, R)$ and its interior contain no equivalents of the origin but for any s > R, $C(\xi, s)$ has such an equivalent in its interior. In this case Sullivan says ξ is a *Garnett point* and we write $\xi \in g$.

A correct form of the theorem is obtained by replacing statement (i) by

$$\xi \notin E \cup g. \tag{i'}$$

A similar correction must be made to Theorem 2 and its corollary.

The author has recently shown that, in general, $g \neq \emptyset$ [2] and Sullivan proves [3] that g has zero one dimensional Lebesgue measure.

REFERENCES

1. P. J. NICHOLLS, Transitive horocycles for Fuchsian groups, Duke Math. J. 42 (1975), 307-312.

3. D. SULLIVAN, On the ergodic theory at infinity of an arbitrary discrete group of hyperbolic motions, Proceedings of Stony Brook Conference on Riemann surfaces and Kleinian groups, June 1978, to appear.

DEPARTMENT OF MATHEMATICS, NORTHERN ILLINOIS UNIV., DE KALB, ILLINOIS 60115

^{2.} P. J. NICHOLLS, Garnett points for Fuchsian groups, to appear in Bull. London Math. Soc.