The (n+20)-th homotopy groups of n-spheres

Dedicated to Professor Y. Akizuki for his 60-th birthday

By

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This paper is a continuation of the calculation of the homotopy groups of spheres in [3]. Denote by S^n the unit n-sphere in euclidean (n+1)-space and by $\pi_r(S^n)$ the r-th homotopy groups of S^n , then $\pi_{n+20}(S^n)$ can be calculated and our results are stated as follows.

Theorem.

$$\begin{split} \pi_{22}(S^2) &\cong Z_{132} \oplus Z_2 \,, \\ \pi_{23}(S^3) &\cong Z_2 \oplus Z_2 \,, \\ \pi_{24}(S^4) &\cong Z_2 \oplus Z_2 \oplus Z_2 \oplus Z_2 \oplus Z_2 \oplus Z_2 \,, \\ \pi_{25}(S^5) &\cong Z_6 \oplus Z_2 \oplus Z_2 \,, \\ \pi_{26}(S^6) &\cong Z_{480} \oplus Z_{12} \,, \\ \pi_{27}(S^7) &\cong Z_{24} \,, \\ \pi_{28}(S^8) &\cong Z_{24} \oplus Z_3 \,, \\ \pi_{29}(S^9) &\cong Z_{24} \,, \\ \pi_{30}(S^{10}) &\cong Z_{504} \oplus Z_{24} \,, \\ \pi_{31}(S^{11}) &\cong Z_{24} \oplus Z_2 \oplus Z_2 \,, \\ \pi_{32}(S^{12}) &\cong Z_{24} \oplus Z_2 \oplus Z_2 \oplus Z_2 \oplus Z_2 \oplus Z_2 \,, \\ \pi_{33}(S^{13}) &\cong Z_{24} \oplus Z_2 \oplus Z_2 \oplus Z_2 \,, \\ \pi_{34}(S^{14}) &\cong Z_{24} \oplus Z_2 \oplus Z_2 \,, \\ \pi_{35}(S^{15}) &\cong Z_{24} \,, \\ \pi_{35}(S^{15}) &\cong Z_{24} \,, \\ \pi_{36}(S^{16}) &\cong Z_{24} \,, \\ \pi_{37}(S^{17}) &\cong Z_{24} \,, \\ \pi_{38}(S^{18}) &\cong Z_{24} \oplus Z_12 \,, \\ \pi_{38}(S^{18}) &\cong Z_{24} \oplus Z_2 \,, \end{split}$$