

## DEGENERATION OF KÄHLER MANIFOLDS

C. H. CLEMENS

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#### INTRODUCTION

Suppose one is given a proper mapping  $p$  of a Kähler manifold  $\mathbf{X}$  onto the unit disc which is of maximal rank except over zero. Then it is an elementary result from algebraic topology that a cohomology class on

$$p^{-1}(t), t \neq 0,$$

which is invariant under the action

$$t = e^{i\theta}, \quad \theta \text{ goes from } 0 \text{ to } 2\pi,$$

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