

MOTIVIC DECOMPOSITION AND INTERSECTION CHOW GROUPS, I

ALESSIO CORTI AND MASAKI HANAMURA

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1. Introduction. We explain our original motivation for writing this paper, then summarise the main results and outline the contents of each section.

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