

REFERENCES

- [1] M. S. BARTLETT, "Complete simultaneous fiducial distributions," *Annals of Math. Stat.*, Vol. X(1939), pp. 129-138.
- [2] W.-V. BEHRENS, "Ein Beitrag zur Fehlerberchnung bei wenigen Beobachtungen," *Landw. Jb.*, Vol. LXVIII(1929), pp. 807-37.
- [3] R. A. FISHER, "The fiducial argument in statistical inference," *Ann. Eugen.*, Vol. VI(1935), pp. 91-98.
- [4] M. S. BARTLETT, The information available in small samples. *Proc. Camb. Phil. Soc.*, Vol. XXXII(1936), pp. 560-66.
- [5] R. A. FISHER, "On a point raised by M. S. Bartlett on fiducial probability," *Ann. Eugen.*, Vol. VIII(1937), pp. 370-75.
- [6] "Student," "The probable error of a mean," *Biometrika*, Vol. VI(1908), pp. 1-25.
- [7] P. V. SUKHATME, "On Fisher and Behrens' test of significance for the difference in means of two normal samples," *Sankhyā*, Vol. IV(1938), pp. 39-48.
- [8] R. A. FISHER, "Samples with possibly unequal variances," *Ann. Eugen.*, Vol. IX(1939), pp. 174-180.
- [9] F. YATES, "An apparent inconsistency arising from tests of significance based on fiducial distributions of unknown parameters," *Proc. Camb. Phil. Soc.* (in press).

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A NOTE ON NEYMAN'S THEORY OF STATISTICAL ESTIMATION¹

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In this note we shall examine a section of a recent paper by Neyman¹ dealing with statistical estimation. Consider the following quotation from that section² which deals with the statement of the problem:

"Consider the variables $[x_1, x_2, \dots, x_n]$ and assume that the form of the probability law $[p(x_1, \dots, x_n | \theta_1, \theta_2, \dots, \theta_t)]$ is known, that it involves the parameters $\theta_1, \theta_2, \dots, \theta_t$ which are constant (not random variables), and that the numerical values of these parameters are unknown. It is desired to estimate one of these parameters, say θ_1 . By this I shall mean that it is desired to define two functions $\bar{\theta}(E)$ and $\theta(E) \leq \bar{\theta}(E)$, determined and single valued at any point E of the sample space, such that if E' is the sample point determined by observation, we can (1) calculate the corresponding values of $\theta(E')$ and $\bar{\theta}(E')$ and (2) state that the true value of θ_1 , say θ_1^0 , is contained within the limits

$$\theta(E') \leq \theta_1^0 \leq \bar{\theta}(E') \quad (18)$$

this statement having some intelligible justification on the ground of the theory of probability.

¹ Specifically we refer to J. Neyman "Outline of a Theory of Statistical Estimation Based on the Classical Theory of Probability," *Phil. Trans. Roy. Soc.*, vol. A236 (1937), pp. 333-380.

² J. Neyman, loc. cit., p. 347. The material in brackets are slight alterations of the original text in order that the quotation do not refer to previous matter in the original paper.