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Comment

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It is indeed very insightful on the part of the editors to put the two papers, one of Reid and the other of Liang and Zeger, together for discussion. For, at first sight, the two papers have little in common. By and large, the first paper has a parametric setup, the other a semiparametric one. Yet the subject matters of the two papers have deeper links which remain to be explored. On one hand, we have results concerning profile likelihood primarily based on parametric models (cf. Cox and Reid, 1987), and on the other hand, we have results based on semiparametric models utilizing optimal estimating function theory. How to compare these two sets of results? This stimulating question has remained largely uninvestigated. Among some exceptions are included the demonstrations of Cox's partial likelihood (Cox, 1975) as the optimal estimating function for a semiparametric model (Godambe, 1985) and similar optimality of the score function obtained from the Cox-Reid (Cox and Reid, 1987) profile likelihood (Godambe, 1991b). Possibly other discussants will provide other examples. Further related comments are given in my discussion of the paper by Liang and Zeger, to follow.

I liked both the papers. However, due to time constraints I will restrict my additional comments only to one paper (Liang and Zeger). I do hope that the two papers and their discussion would stimulate further research in the problem area (briefly mentioned above) implied by the papers.

Liang and Zeger have a lucid style of presentation. With properly selected examples they first illustrate how the existence of nuisance parameters can affect inference about the parameter of interest. Using the same examples they later demonstrate how the effect of the nuisance parameters can be reduced or eliminated using estimating function theory. All this is accomplished at a common level of understanding. This paper therefore has both scientific and pedagogical value.

The following comments are meant to clarify and emphasize some points in the paper which perhaps have not received enough attention.

In Section 2.4, the authors state that a major limitation of estimating function theory is that it ascribes optimality to the estimating function, while scientists and practitioners are concerned about estimators. They quote Crowder's remark "This is like admiring the pram rather than the baby" (Crowder, 1989), from the discussion of the paper of Godambe and Thompson (1989); these authors' reply to Crowder, not reproduced in the present paper, is given below with some elaboration. I hope this will remove some misunderstanding about an important aspect of the subject.

How good is the estimate? Conventionally the question is answered in terms of the "error" of the estimator. Now the concept of error is somewhat complicated and does not admit a simple definition. Certainly error is not just a root of an arbitrary (unbiased or nearly so) estimate of variance. In parametric inference, however, the practice is fairly clear. For a parametric model, the error is derived from the natural estimate of the variance of the score function. The error is the inverse of the square root of observed Fisher information (Efron

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