

CORRECTION NOTE

CORRECTION TO

"ON DISTINGUISHING TRANSLATES OF MEASURES"

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The proof of Theorem 3 of [1] contains a gap which we fill with the three Lemmas that follow. We also note that $f_N(x)$ should be changed to $f_N(x + \alpha m)$ on page 1776 of [1], line 21, where $f_N(x)$ is defined.

Our notation is the same as in [1]. The setting is, as before, a general real stochastic process $X = (X(t) | t \in T)$. We let S stand for the set of all real valued functions on T and we let \mathcal{A} stand for the σ -field of subsets of S generated by coordinates. For a fixed element $m \in S$ and $\alpha \in R$, the real line, we let P_α stand for the measure induced on (S, \mathcal{A}) by the process $(X(t) + \alpha m(t) | t \in T)$.

We say that the measures P_α are *simultaneously Borel* distinguishable if there exists an \mathcal{A} measurable function f such that

$$P_\alpha[f = \alpha] = 1 \quad \text{for all } \alpha \in R.$$

In our earlier paper [1] we called the parameter α "consistently" distinguishable in this case, a terminology which seems at variance with the usual terminology which reserves the term "consistently" for the convergence (a.s.) or in probability of "finitely defined" functionals to the true parameter α .

LEMMA 1. Let $(X_n | n \geq 1)$ be a sequence of independent identically distributed random variables. Suppose $m = (m_n | n \geq 1)$ is a sequence of real numbers such that $\sup_{n \geq 1} |m_n| = \infty$. Then there exists a sequence f_k of \mathcal{A} measurable linear functionals defined on S such that

$$f_k(x + \alpha m) \rightarrow \alpha \quad \text{a.s. } \forall \alpha.$$

PROOF. Pick a subsequence n_k such that $|m_{n_k}| \rightarrow \infty$. For

$$x = (x_1, x_2, \dots) \in S$$

define

$$f_k(x) = x_{n_k} / m_{n_k}.$$

Now

$$(X_{n_k} + \alpha m_{n_k}) / m_{n_k} = \alpha + X_{n_k} / m_{n_k}.$$

Also it is clear that

$$X_{n_k} / m_{n_k} \rightarrow 0 \quad \text{a.s.},$$

taking a subsequence if necessary. It follows that

$$f_k(x + \alpha m) \rightarrow \alpha \quad \text{a.s. } \forall \alpha. \quad \square$$

LEMMA 2. Let $(X_n | n \geq 1)$ be a sequence of independent identically distributed