

where $\alpha_k = N$, $\alpha_0 = 0$. This is the distribution of cell frequencies in a p by k contingency table with all totals fixed when there is independence (see [1], p. 278) and thus, for large values of m_{ij} at least, the usual chi-square test can be used.

REFERENCE

- [1] A. M. Mood, *Introduction to the Theory of Statistics*, McGraw-Hill Book Co., 1950.

AN OMISSION IN NORTON'S LIST OF 7×7 SQUARES

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1. In a previous paper the value 16,942,080 for the number of reduced 7×7 squares was obtained by the author by an exhaustive method, subject to a strict control ([4], Section 20). This number exceeds Norton's ([2], Table on p. 290) by 14,112. An attempt was made in Section 21 of [4] to show that this discrepancy in the total number does not affect Norton's conjecture ([2], p. 291) that the 146 species represent the whole of the universe of 7×7 Latin squares. However, R. A. Fisher has informed the author that the discrepancy cannot be explained away in this manner. It has therefore to be attributed to a gap in Norton's list.

2. Now, a 147th species containing 14,112 squares can arise only from an automorph type through an operator of the order 5^k . It is easy to construct a matrix Q corresponding to such an operator as, for example, $T = (34567)^3$. Here the cycle (34567) signifies a permutation [1] of columns, a permutation of rows and a substitution of elements.

The first two rows of Q are respectively identical with the first two columns and define the substitution (12) (34567). In the remaining 5×5 squares, it is necessary that the elements of the broken diagonals follow in the natural cyclic order, except the numbers 1 and 2, which each form a broken diagonal.

The square is given below:

$$Q = \begin{array}{ccccccc} 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ 2 & 1 & 4 & 5 & 6 & 7 & 3 \\ 3 & 4 & 5 & 7 & 1 & 2 & 6 \\ 4 & 5 & 7 & 6 & 3 & 1 & 2 \\ 5 & 6 & 2 & 3 & 7 & 4 & 1 \\ 6 & 7 & 1 & 2 & 4 & 3 & 5 \\ 7 & 3 & 6 & 1 & 2 & 5 & 4. \end{array}$$

3. On replacing each row of Q by the conjugate permutation and rotating the figure through an angle of 180° about the diagonal, we obtain the square