

to be subject to certain indeterminate errors." This remark was intended simply to call attention to the discussion of the accuracy of the table made by the authors of [9] and should not discourage the use of the table since the present writer was merely referring to the evaluation of accuracy made by the authors themselves.

Meanwhile Dr. Churchill Eisenhart has pointed out that an exact table for the case of two degrees of freedom ( $r = 0$ ) has been added to reference [1] as printed in *Contributions to Mathematical Statistics* by R. A. Fisher (John Wiley and Sons, 1950).

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### ABSTRACTS OF PAPERS

(Abstracts of papers presented at the Chicago meeting of the Institute,  
December 27-30, 1952)

1. **A Two-Sample Multiple Decision Procedure for Ranking Means of Normal Populations with Unknown Variances. (Preliminary Report.)** ROBERT E. BECHHOFFER, CHARLES W. DUNNETT AND MILTON SOBEL, Cornell University.

The multiple decision problem of ranking  $k$  normal populations according to their population means when both the means and the variances are unknown is considered. Useful confidence statements, which are independent of the unknown variances, can be made concerning the rankings if a generalized Stein two-sample procedure is used. The rankings are of the general type formulated by Bechhofer (*Ann. Math. Stat.*, Vol. 23 (1952), p. 139), which includes selecting the population with the largest population mean and ranking completely all  $k$  populations. Two cases are considered: A) population variances unknown and equal, and B) population variances unknown and not necessarily equal. To determine the size (which may be zero) of the second sample, tables for a  $(k - 1)$ -variate analogue of Student's  $t$ -distribution are required for case A, and tables for a  $(k - 1)$ -variate analogue of the distribution of the difference between two independent Student  $t$ -statistics are required for case B. For  $k = 2$ , tables due to Fisher and Sukhatme are available for cases A and B, respectively. For case A,  $k = 3$ , tables are being computed. For case A,  $k > 3$  and for case B,  $k \geq 3$ , computation of the necessary tables is contemplated. (This research was sponsored by Air Research and Development Command.)

2. **A Sequential Multiple Decision Procedure for Ranking Means of Normal Populations with Known Variances. (Preliminary Report.)** ROBERT E. BECHHOFFER AND MILTON SOBEL, Cornell University.

Let  $X_{ij}$  be normally and independently distributed  $N(X_{ij} | \mu_i, \sigma^2)$  from population  $\pi_i$  ( $i = 1, \dots, k; j = 1, 2, \dots$ ). The  $\mu_i$  are unknown;  $\sigma^2$  is known. Denote the ranked  $\mu_i$  by  $\mu_{[1]} < \dots < \mu_{[k]}$ . It is desired to choose the population with mean  $\mu_{[k]}$ . Denote the sample sum based on  $m$  observations from  $\pi_i$  by  $Q_{im} = \sum_{j=1}^m x_{ij}$ ; denote the ranked  $Q_{im}$  by  $R_{1m} < \dots < R_{km}$ . Define  $y_m = R_{km} - R_{k-1,m}$  ( $m = 1, 2, \dots$ ) and  $\delta_{k,i} = \mu_{[k]} - \mu_{[i]}$  ( $i = 1, \dots, k - 1$ ). Let  $\delta^* > 0$  be the smallest value of  $\delta_{k,k-1}$  that it is desired to detect, and let  $1 - \beta(1/k < 1 - \beta < 1)$  be the desired probability of a correct choice (p.c.c.)