

## CORRECTION NOTES

### CORRECTION TO

#### “A REMARK ON NONATOMIC MEASURES”

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The “only if” part of the theorem proved in this note (*Ann. Math. Statist.* **43** (369–370)) is not correct. Here is an example.

Let  $I^2$  be the unit square equipped with the usual Borel  $\sigma$ -algebra. Let  $\mu$  and  $\lambda$  be two continuous measures on  $I^2$  with total mass  $\frac{1}{2}$  each concentrated on the lines  $x = \frac{1}{2}$  and  $y = \frac{1}{2}$  respectively.  $\mu + \lambda$  is nonatomic on  $I^2$  but none of the marginals is nonatomic. In fact,  $\{\frac{1}{2}\}$  is a measure atom for both the marginals.

Remark (1) is also not true. The Cantor set  $\{0, 1\}^{\aleph_0}$  with Haar measure is the counter example.

### CORRECTION TO

#### “THE WEIGHTED LIKELIHOOD RATIO, SHARP HYPOTHESES ABOUT CHANCES, THE ORDER OF A MARKOV CHAIN”

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The claim (Section 3.3) in our paper (*Ann. Math. Statist.* **41** 214–226) of the invariance of Savage’s Density Principle,

$$(2.20) \quad g(\zeta) = f(\eta_0, \zeta) / \int f(\eta_0, \tilde{\zeta}) d\tilde{\zeta}$$

is fallacious; hence if Savage’s Density Ratio (equation (2.21)) holds for one parametrization, it need not hold for the induced density under a new parametrization. In equation (3.30) of our “proof”, the first equality holds if  $J(\partial\eta/\partial\eta^*)(\eta_0, \zeta)$  is constant in  $\zeta$ . For the given log-odds example,  $\partial\eta/\partial\eta^* = \zeta$  (read  $\zeta^* = \frac{1}{2} \log(\theta_1/\theta_2)$ ).

Seymour Geisser and a referee have asked us about invariance. In the last weeks of his life, Leonard J. Savage, called our attention to the Borel-Kolmogorov paradox (Kolmogorov, *Foundations of Probability*, Chapter V, Section 2), whereby a conditional distribution depends on not just the conditioning event, but also on the parameter defining the event.