Comment: Quantifying the Fraction of Missing Information for Hypothesis Testing in Statistical and Genetic Studies

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Nicolae, Meng and Kong are to be congratulated on having treated an important practical problem in many scientific inquiries in which the investigator has chosen the testing procedure, but needs to know the impact of the missing data on the test in terms of the relative loss of information. To measure the relative information, they propose to compare how the observed-data likelihood deviates from flatness relative to the same deviation in the complete-data likelihood. Several measures of this deviation expressed by Bayesian method are explored and applied to the study of genetics and genomics. As noted in their paper, these measures are especially needed in small-sample problems with incomplete data.

We would like to explore the use of this type of measure in two examples to indicate its wide applicability and some computational issues. One concerns infectious disease data, which are usually highly dependent and incomplete; the investigators often need to decide if more data are needed, and in case they are, to know the type of data that is most desirable. The other concerns a test on the shape of a regression function; we will apply the Bayesian measure of relative information to select design points for collecting more data. Because Bayesian tests are more tractable and natural than a frequentist approach in these two examples, we consider the following extensions of their (25) for the measure of relative information:

\[
E_0 \left\{ \text{Var} \left[ \text{lod}(\theta, \theta | Y_{ob}) \middle| Y_{ob} \right] \right\} \cdot \left( E_0 \left\{ \text{Var} \left[ \text{lod}(\theta, \theta | Y_{ob}) \middle| Y_{ob} \right] \right\} + \text{Var} \left[ \log \left( \frac{P(Y_{co} | Y_{ob}, \theta)}{P(Y_{co} | Y_{ob}, \theta_0)} \middle| Y_{ob} \right) \right] \right) \right)^{-1}
\]

\[
E_0 \left\{ \text{Var} \left[ \text{lod}(\theta_0, \theta | Y_{ob}) \middle| Y_{ob} \right] \right\}
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