

Erratum

Erratum to “On Integral Inequalities of Hermite-Hadamard Type for s -Geometrically Convex Functions”

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In [1, Definition 1.9], the concept “ s -geometrically convex function” was introduced where

Making use of [1, Lemma 2.1], Hölder’s integral inequality, and other analytic techniques, some inequalities of Hermite-Hadamard type were established. However, there are some vital errors appeared in main results of the paper [1].

The aim of this paper is to correct these errors and we now start off to correct them.

Correction to Theorem 3.1. Let $f : I \subset \mathbb{R}_+ \rightarrow \mathbb{R}$ be a differentiable function on I° such that $f' \in L([a, b])$ for $0 < a < b < \infty$. If $|f'(x)|^q$ is s -geometrically convex and monotonically decreasing on $[a, b]$ for $q \geq 1$ and $s \in (0, 1]$, then

$$\left| f\left(\frac{a+b}{2}\right) - \frac{1}{b-a} \int_a^b f(x) dx \right| \leq \frac{b-a}{4} \left(\frac{1}{2}\right)^{1-1/q} G_1(s, q; g_1(\alpha), g_2(\alpha)), \quad (1)$$

$$\left| \frac{f(a)+f(b)}{2} - \frac{1}{b-a} \int_a^b f(x) dx \right| \leq \frac{b-a}{4} \left(\frac{1}{2}\right)^{1-1/q} G_1(s, q; g_2(\alpha), g_1(\alpha)), \quad (2)$$

$$g_1(\alpha) = \begin{cases} \frac{1}{2}, & \alpha = 1, \\ \frac{\alpha \ln \alpha - \alpha + 1}{\ln^2 \alpha}, & \alpha \neq 1, \end{cases} \quad (3)$$

$$g_2(\alpha) = \begin{cases} \frac{1}{2}, & \alpha = 1, \\ \frac{\alpha - \ln \alpha - 1}{\ln^2 \alpha}, & \alpha \neq 1, \end{cases}$$

$$\alpha = \left| \frac{f'(b)}{f'(a)} \right|^{sq/2}, \quad (4)$$

$G_1(s, q; g_1(\alpha), g_2(\alpha))$

$$= \begin{cases} |f'(a)|^s [g_1(\alpha)]^{1/q} + |f'(a) f'(b)|^{s/2} \times [g_2(\alpha)]^{1/q}, & |f'(a)| \leq 1, \\ |f'(a)| [g_1(\alpha)]^{1/q} + |f'(a)|^{1-s/2} \times |f'(b)|^{s/2} [g_2(\alpha)]^{1/q}, & |f'(b)| \leq 1 \leq |f'(a)|, \\ |f'(a)| |f'(b)|^{1-s} [g_1(\alpha)]^{1/q} + |f'(a) f'(b)|^{1-s/2} \times [g_2(\alpha)]^{1/q}, & 1 \leq |f'(b)|. \end{cases} \quad (5)$$