

# Proof of a conjecture of F. Nevanlinna concerning functions which have deficiency sum two

by

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In memoriam:

Frithiof Nevanlinna (1894–1977)

Rolf Nevanlinna (1895–1980)

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