

## Correction to “Uniformization of Kähler manifolds with vanishing Bochner tensor”

by

YOSHINOBU KAMISHIMA

*Tokyo Metropolitan University  
Tokyo, Japan*

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In [2], we discussed the uniformization of Kähler manifolds with vanishing Bochner tensor, called Bochner–Kähler or Bochner-flat manifolds. The resulting uniformization theorem, Theorem A, was used to classify compact Bochner-flat Kähler manifolds. In Theorem A, we claimed that every Bochner-flat Kähler manifold is uniformized by one of four types of Hermitian symmetric space. Subsequent work by R. Bryant [1] has revealed that this statement is false and that there are many Bochner-flat Kähler manifolds which are not locally symmetric. In the compact case, however, the statement of our classification result turned out to be correct, and a proof was given in [1].

In order to explain the error and to indicate how it might be corrected, let us recall the argument. The main idea, due to Webster [3], is to observe that over any simply-connected domain  $U$  in a Kähler  $2n$ -manifold  $M$ , there is a  $CR$  structure on  $p: U \times \mathbf{R} \rightarrow M$  whose contact form  $\omega$  satisfies  $d\omega = p^*\Omega$ , where  $\Omega$  is the Kähler form of  $M$ . The contact distribution  $\ker \omega$  is transverse to the fibres of  $p$  and is equipped with the lift of the complex structure on  $TM$ . There is a natural fibrewise  $\mathbf{R}$ -action by  $CR$  automorphisms.

If  $M$  is Bochner-flat, it follows from [3] that this  $CR$  structure is spherical, and therefore there is a developing map  $\text{dev}: U \times \mathbf{R} \rightarrow S^{2n+1}$ , together with an induced group homomorphism  $\varrho: \mathbf{R} \rightarrow PU(n+1, 1)$  into the group of  $CR$  automorphisms of  $S^{2n+1}$ . This pair is uniquely determined up to  $CR$  automorphism. We let  $G$  denote the closure of  $\varrho(\mathbf{R})$  and  $X$  the complement of its fixed-point set in  $S^{2n+1}$ : since the natural fibrewise  $\mathbf{R}$ -action is free and  $\text{dev}$  is an immersion, it follows that  $\text{dev}(U \times \mathbf{R}) \subset X$ .

If we have a good open cover  $U_\alpha$  of  $M$ , we have developing pairs  $(\text{dev}_\alpha, \varrho_\alpha)$  related by  $CR$  automorphisms on pairwise intersections, and (assuming that  $M$  is connected),