

THE NUMBER OF HOMEOMORPHICALLY IRREDUCIBLE TREES, AND OTHER SPECIES

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1. Introduction

Our object is to augment the already rich literature on the enumeration of trees by the addition of several previously uncounted species. Interest is moreover derived from the fact that we use variations of one general method in each of these cases; a method which is also applicable to numerous counting problems not treated in this paper (e.g., see Riordan

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