

SOME ASPECTS OF GROUPS WITH UNIQUE ROOTS

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Introduction

1. The multiplicative notation employed in the study of groups leads, in a natural way to the notion of roots in groups. Thus if n is a positive integer and g is an element of a group G then a solution x of the equation

$$x^n = g$$