

# Unitary derived functor modules with small spectrum

by

T. J. ENRIGHT<sup>(1)</sup>

*University of California, San Diego  
La Jolla, CA, U.S.A.*

R. PARTHASARATHY

*Tata Institute of Fundamental Research  
Bombay, India*

and

N. R. WALLACH<sup>(1)</sup>

*Rutgers University  
New Brunswick, N.J., U.S.A.*

J. A. WOLF<sup>(1)</sup>

*University of California  
Berkeley, CA, U.S.A.*

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## § 1. Introduction

For a real semisimple Lie group  $G$ , the description of the unitary dual remains an elusive question. One of the difficulties has been the lack of technique for constructing

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