

## Correction to

On the Diophantine equation  $1^k + 2^k + \dots + x^k + R(x) = y^2$

by

M. VOORHOEVE, K. GYÖRY and R. TIJDEMAN

*Technische Universiteit Eindhoven, Netherlands*    *University of Debrecen Debrecen, Hungary*    *Rijksuniversiteit Leiden Leiden, Netherlands*

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In the above article the authors claim that a polynomial  $P$  with rational integer coefficients which is congruent (mod 4) to

$$3x^8 + 2x^6 + x^4 + 2x^2$$

has at least three simple roots. Their argumentation is incorrect. In this corrigendum, they wish to repair this defect by proving claim (i) in case B of Lemma 4 in a correct way.

Suppose  $P$  can be written as

$$P(x) \equiv Q(x)T^2(x), \quad (*)$$

with  $\deg Q \leq 2$ .

If  $\deg Q = 0$ , then clearly  $Q$  is an odd constant, so  $T^2(x) \equiv x^8 + x^4 \pmod{2}$ , hence  $T(x) \equiv x^4 + x^2 \pmod{2}$  and  $T^2(x) \equiv x^8 + 2x^6 + x^4 \pmod{4}$ , which is clearly not the case. If  $\deg Q = 1$ , then either  $Q(x) \equiv x$  or  $Q(x) \equiv x + 1 \pmod{2}$ . In both cases, the quotient of  $P$  and  $Q$  cannot be written as a square (mod 2). If  $\deg Q = 2$ , then either

$$Q(x) \equiv x^2 \quad \text{or} \quad Q(x) \equiv x^2 + x \quad \text{or} \quad Q(x) \equiv x^2 + 1 \pmod{2},$$

since  $x^2 + x + 1$  does not divide  $P \pmod{2}$ . In the first case  $T(x) \equiv x^3 + x \pmod{2}$ , hence  $T^2(x) \equiv x^6 + 2x^4 + x^2 \pmod{4}$  which does not divide  $P \pmod{4}$ . In the second case, the