

a dense subset, in the fine  $C^0$  topology, of the set of topological imbeddings of  $U$  into  $l_2$ .

The proof of this theorem, which requires the alternative form of Theorem 1, is similar to the proof of Theorem 2 and is therefore omitted. The principal modification needed consists in allowing the maps  $F_{c,r,i,j,m}$ , (which are now defined on  $l_2$  in the obvious way using (9)–(9)'), to act now on the left of the imbeddings via a suitably defined infinite left composition, and where the positive integer  $j$  is not subject to the condition  $j \leq n$  of Theorem 2.

Correction to

## DIMENSION THEORY IN POWER SERIES RINGS

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While recently answering a letter of inquiry of T. Wilhelm, I discovered an error in Corollary 4.6. The result, as originally stated, clearly requires that  $P \cdot V[[X]] \subset P[[X]]$ . However, if  $P$  is not branched, it is possible that  $P \cdot V[[X]] = P[[X]]$ ; a counterexample can be obtained from Proposition A.

The following modification of Corollary 4.6 is sufficient for the proof of Theorem 4.7.

**COROLLARY 4.6'.** *Let  $V$  be a valuation ring having a proper prime ideal  $P$  which is branched. If  $P$  is idempotent, then there is a prime ideal  $Q$  of  $V[[X]]$  which satisfies  $P \cdot V[[X]] \subseteq Q \subset P[[X]]$ .*

*Proof.* Since  $P$  is branched, there is a prime ideal  $\bar{P}$  of  $V$  with  $\bar{P} \subset P$  and such that there are no prime ideals of  $V$  properly between  $\bar{P}$  and  $P$  [1; 173]. By passing to  $V[[X]]/\bar{P}[[X]] (\cong (V/\bar{P})[[X]])$ , we may assume that  $P$  is a minimal prime ideal of  $V$ .

Since  $P$  is idempotent,  $PV_P$  is idempotent by Lemma 4.1; hence  $V_P$  is a rank one nondiscrete valuation ring. By Theorem 3.4, there is a prime ideal  $Q$  of  $V_P[[X]]$  such that  $(PV_P) \cdot V_P[[X]] \subseteq Q \subset (PV_P)[[X]]$ . But then we see that  $Q \subset (PV_P)[[X]] = P[[X]] \subseteq V[[X]]$ . Hence  $Q \cap V[[X]] = Q$  and  $Q$  is a prime ideal of  $V[[X]]$  with  $P \cdot V[[X]] \subseteq Q \subset P[[X]]$ .

The following result is now of interest.

**PROPOSITION A.** *Let  $V$  be a valuation ring having a proper prime ideal  $P$  which is not branched; then  $P = \bigcup_{\lambda \in A} M_\lambda$ , where  $\{M_\lambda\}_{\lambda \in A}$  is the collection of prime ideals of  $V$  which are properly contained in  $P$ . In this case,  $P \cdot V[[X]] = P[[X]]$  if and only if (\*) given any countable subcollection  $\{M_{\lambda_i}\}$  of  $\{M_\lambda\}$ ,  $\bigcup_{i=1}^{\infty} M_{\lambda_i} \subset P$ .*

*Proof.* Assuming (\*), let  $f(X) = \sum_{i=0}^{\infty} f_i X^i \in P[[X]]$ . For each  $i$ ,  $f_i \in M_{\bar{\lambda}_i}$  for some  $\bar{\lambda}_i \in A$ . Let  $p \in P$ ,  $p \notin \bigcup_{i=0}^{\infty} M_{\bar{\lambda}_i}$ ; since  $p \notin M_{\bar{\lambda}_i}$ , it follows that  $f_i \in M_{\bar{\lambda}_i} \subseteq (p)V$  for each  $i$  and  $f(X) \in (p)V[[X]] \subseteq P \cdot V[[X]]$ .

Conversely, assuming that (\*) fails, let  $\{M_{\lambda_i}\}_{i=1}^{\infty}$  be a countable subcollection of  $\{M_\lambda\}_{\lambda \in A}$  such that  $\bigcup_{i=1}^{\infty} M_{\lambda_i} = P$ . By extracting a subsequence of  $\{M_{\lambda_i}\}$ , we may assume that  $M_{\lambda_i} \subset M_{\lambda_{i+1}}$  for each  $i$ . Let  $f_i \in M_{\lambda_{i+1}}$ ,  $f_i \notin M_{\lambda_i}$  and let  $f(X) = \sum_{i=1}^{\infty} f_i X^i$ ; then  $f(X) \in P[[X]]$  but  $f(X) \notin P \cdot V[[X]]$ .

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Correction to

## COHOMOLOGY OF FINITELY PRESENTED GROUPS

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In the second paragraph of the abstract, p. 615, the first sentence, "If  $G$  is generated by  $n$  elements, ..." should read "If  $G$  is a residually finite group generated by  $n$  elements, ...".

Correction to

## COMMUTANTS OF SOME HAUSDORFF MATRICES

B. E. RHOADES

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In [2] it is shown that, for  $A$  a conservative triangle,  $B$  a matrix with finite norm commuting with  $A$ ,  $B$  is triangular if and only if

(1) for each  $t \in l$  and each  $n$ ,  $t(A - a_{nn}I) = 0$  implies  $t$  belongs to the linear span of  $(e_0, e_1, \dots, e_n)$ . On page 716 of [2] it is asserted that

(2)  $(U^*)^{n+1}(A - a_{nn}I)U^{n+1}$  of type  $M$  for each  $n$  is equivalent to