# THE ANNALS of

### **PROBABILITY**

## AN OFFICIAL JOURNAL OF THE INSTITUTE OF MATHEMATICAL STATISTICS

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