

## Erratum

# On the Spectra of Randomly Perturbed Expanding Maps

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The authors wish to point out an error in Sublemma 6 in Sect. 5 of [1]. The claims in Theorems 3 and 3' have been revised accordingly; a correct version is given below. Other results in [1] are not affected.

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### i) Revised Statement of Results in Sect. 5.C

Section 5 of [1] is about piecewise  $C^2$  expanding mixing maps  $f$  of the interval. The number  $\Theta$  below refers to  $\Theta = \lim_{n \rightarrow \infty} \sup(1/|(f^n)'|^{1/n})$ . These maps are randomly perturbed by taking convolution with a kernel  $\theta_\varepsilon$ , and the resulting Markov chain is denoted  $\chi^\varepsilon$ . The piecewise statements of Theorems 3 and 3' should read as follows:

**Theorem 3.** *Let  $f: I \rightarrow I$  be as described in Sect. 5.A of [1], with a unique absolutely continuous invariant probability measure  $\mu_0 = \rho_0 \, dm$ , and let  $\chi^\varepsilon$  be a small random perturbation of  $f$  of the type described in Sect. 5.B with invariant probability measure  $\rho_\varepsilon \, dm$ . We assume also that  $f$  has no periodic turning points. Then*

- (1) *The dynamical system  $(f, \mu_0)$  is stochastically stable under  $\chi^\varepsilon$  in  $L^1(dm)$ , i.e.,  $|\rho_\varepsilon - \rho_0|_1$  tends to 0 as  $\varepsilon \rightarrow 0$ .*

*Let  $\tau_0 < 1$  and  $\tau_\varepsilon < 1$  be the rates of decay of correlations for  $f$  and  $\chi^\varepsilon$  respectively for test functions in  $BV$ . Then:*

- (2)  $\limsup_{\varepsilon \rightarrow 0} \tau_\varepsilon \leq \sqrt{\tau_0}$ .

**Theorem 3'.** *Let  $f$  and  $\chi^\varepsilon$  be as in Theorem 3, except that we do not require that  $f$  has no periodic turning points. Then*

- (1)  $|\rho_\varepsilon - \rho_0|_1$  tends to 0 as  $\varepsilon \rightarrow 0$  if  $2 < 1/\tau_0 \leq 1/\Theta$ ;
- (2)  $\limsup_{\varepsilon \rightarrow 0} \tau_\varepsilon \leq \sqrt{2\tau_0}$ .