The nature of the constant  $A_4$  here remains undetermined just as in the papers of Rutledge and Douglass. Whether or not it can be rationally expressed in terms of the constants  $s_1$ ,  $\sigma_1$ ,  $s_3$  and  $\pi$  is an open question. Some light may be thrown on the problem by a further study of the function  $\xi_1(x)$  treated briefly by Nielsen.\* His definition is as follows,

(36) 
$$\xi_1(x) = \int_0^1 \frac{\log (1+t)}{1+t} t^{x-1} dt, \qquad R(x) > 0.$$

From this equation and (27) it follows that

(37) 
$$A_4 = 5s_4/16 - \xi_1^{(2)}(1).$$

This in itself, of course, sheds no light but if a relation analogous to (16) could be found involving the function  $\xi_1(x)$ , it would seem that the question could be answered.

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## THE COMPUTATION OF THE SMALLER COEFFICIENTS OF $J(\tau)$

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The purpose of this note is to call attention to the fact that the first twenty-five coefficients  $a_0, a_1, \cdots, a_{24}$  in the expansion

(1) 
$$1728J(\tau) = e^{-2\pi i\tau} + \sum_{n=0}^{\infty} a_n e^{2\pi i n\tau}$$

can be computed with relative ease, making use of H. Gupta's tables<sup>‡</sup> of the partition function which extend to n = 600.

From the multiplicator equation § of fifth order of  $J(\tau)$  we have

(2) 
$$\begin{array}{r} 1728J(\tau) = y^{-1} + 6 \cdot 5^3 + 63 \cdot 5^5 y + 52 \cdot 5^8 y^2 + 63 \cdot 5^{10} y^3 \\ + 6 \cdot 5^{13} y^4 + 5^{15} y^5 . \end{array}$$

with

<sup>\*</sup> N. Nielsen, loc. cit., p. 233.

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<sup>‡</sup> A table of partitions, Proceedings of the London Mathematical Society, vol. 39 (1935), pp. 142–149; A table of partitions II, Proceedings of the London Mathematical Society, vol. 42 (1937), pp. 546–549.

<sup>§</sup> Klein-Fricke, Vorlesungen über die Theorie der elliptischen Modulfunktionen, vol. 2, p. 61, formula (11), with the values given in vol. 2, p. 64, (5) and vol. 1, p. 154, (1).