

G is less than $\frac{1}{2}(t^2 - t + 6) + \varepsilon(t - 1) + (t + \varepsilon)!/\varepsilon!$ unless the class is less than $n - 2t + 3$.

The inequality

$$\frac{n(n-1) \cdots (n-t+1)(n-t-\varepsilon)(n-t-\varepsilon-2) \cdots (n-3t-\varepsilon+4)}{n(n-1) \cdots (n-2t+6)(n-2t+5)} \leq \frac{(t+\varepsilon)!}{\varepsilon!}$$

where $0 \leq \varepsilon \leq t - 3$, is found as before, and from it the theorem follows.

3.

Another theorem of value in the applications is the following :

THEOREM IV. *A doubly transitive group cannot contain an invariant imprimitive subgroup unless its degree is a power of a prime. Then the group is a subgroup of the holomorph of the abelian group of order p^a and type $(1, 1, \dots)$.*

On pages 193 and 194 of his *Theory of Groups* Burnside proves that the invariant imprimitive subgroup H is of degree n and class $n - 1$ and that the $n - 1$ substitutions of degree n in H form a single conjugate set under G . Then by Frobenius's theorem on groups of "class $n - 1$," H contains a characteristic subgroup of degree and order n which is abelian with all its operators of the same order.

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DIFFERENTIAL GEOMETRY OF n DIMENSIONAL SPACE.

Sur les Systèmes Triplement Indéterminés et sur les Systèmes Triple-Orthogonaux. Par C. GUICHARD. Scientia, no. 25. Gauthier-Villars, Paris, 1905. viii + 95 pp.

DURING the past ten years the field of differential geometry has been greatly enriched by the researches of M. Guichard. The eminent geometer has made a profound study of the properties of ordinary space by means of operations defined for space of n dimensions. He has introduced two elements depending upon two variables; they are the *resseau* and the *congruence*. By definition, a point of space in n dimensions