Complex Hypersurfaces in an Indefinite Complex Space Form

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Introduction

Let $M_s^n(c)$ be an n $(n \ge 2)$ -dimensional indefinite complex space form of constant holomorphic curvature c and of index 2s. Recently Romero [5] proved that an indefinite complex hypersurface with parallel Ricci tensor in $M_{s+a}^{n+1}(c)$ $(c \ne 0)$ is Einstein. The purpose of this paper is to study an indefinite complex hypersurface M in $M_{s+a}^{n+1}(c)$ satisfying the condition

$$(*) R(X, Y)S=0,$$

for any vector fields X and Y of M, where R denotes the curvature tensor, S is the Ricci tensor and R(X, Y) operates on the tensor algebra as a derivation. We shall prove the following

THEOREM. Let M be a complex hypersurface of index 2s in $M_{s+a}^{n+1}(c)$ $(n \ge 2)$. If $c \ne 0$ and M satisfies the condition (*), then M is Einstein.

In the last section it is shown that there exist many examples of Einstein complex hypersurfaces in an indefinite complex Euclidean space different from those given by Romero [3].

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§1. Complex hypersurfaces in an indefinite complex space form.

Let M be a complex m-dimensional indefinite Kaehlerian manifold. Then M is equipped with an almost complex structure J which is

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