

ON BOREL SUMMATION AND STOKES PHENOMENA FOR RANK-1 NONLINEAR SYSTEMS OF ORDINARY DIFFERENTIAL EQUATIONS

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1. Introduction. In this paper we study analytic (linear or) nonlinear systems of ordinary differential equations (ODEs), at an irregular singularity of rank-1,

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